

# Towards Understanding of the Behavior of Web Streaming

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**Abstract**—We study the behavior of a modern-era adaptive streaming system delivering videos embedded in web-pages. In such an application, the size of videos rendered on the screen may depend on user preferences, such as the position and size of a browser window. Moreover, the stream selection logic in such a system appears to be influenced not only by the available network bandwidth but also by the output video size, which, in many cases, limits the selection of higher quality streams. To explain this behavior, in this paper we introduce a simple analytical model of a client adapting to both bandwidth and player size. Using this model, we then compute stream selection probabilities and show that they are sufficiently close to respective statistics observed in practical experiments. Possible uses of this proposed client model are also suggested. Specifically, we show how it can be used to derive formulae for the average performance parameters of the system and also for posing related optimization problems.

**Keywords**—ABR streaming, encoding ladder, stochastic models, average-case analysis, non-linear constrained optimization

## I. INTRODUCTION

### A. The behavior of adaptive streaming

Continuous playback under unknown or dynamically changing network conditions was the first and arguably most

fundamental problem that early Internet streaming systems have tried to address [1-3]. An early example of a satisfactory solution was the so-called “SureStream” technology, introduced by RealNetworks in 1998 [3]. The main idea was to encode media at multiple bitrates and design a system switching between such streams adaptively, as needed to match network bandwidth, observable at each point in time. The same basic concept is well known today as *Adaptive Bitrate Streaming*, providing the basis for modern streaming protocols and standards such as HLS [4] and DASH [5]. In all such recent systems, the decisions about stream selections are usually done by *streaming clients*, running on user devices.

Moreover, in the modern days of streaming, and specifically in streaming to web browsers, there is another important parameter affecting the playback. It is the *size of a video player window* or *video display area* on a webpage. What causes its variation are user preferences, influencing the position and size of the browser window on the screen, as well as form factor/display size of the user device.

To illustrate the significance of this parameter, in Fig. 1, we show playback statistics captured during a large scale web streaming event. In Table 1, we also list the parameters of the

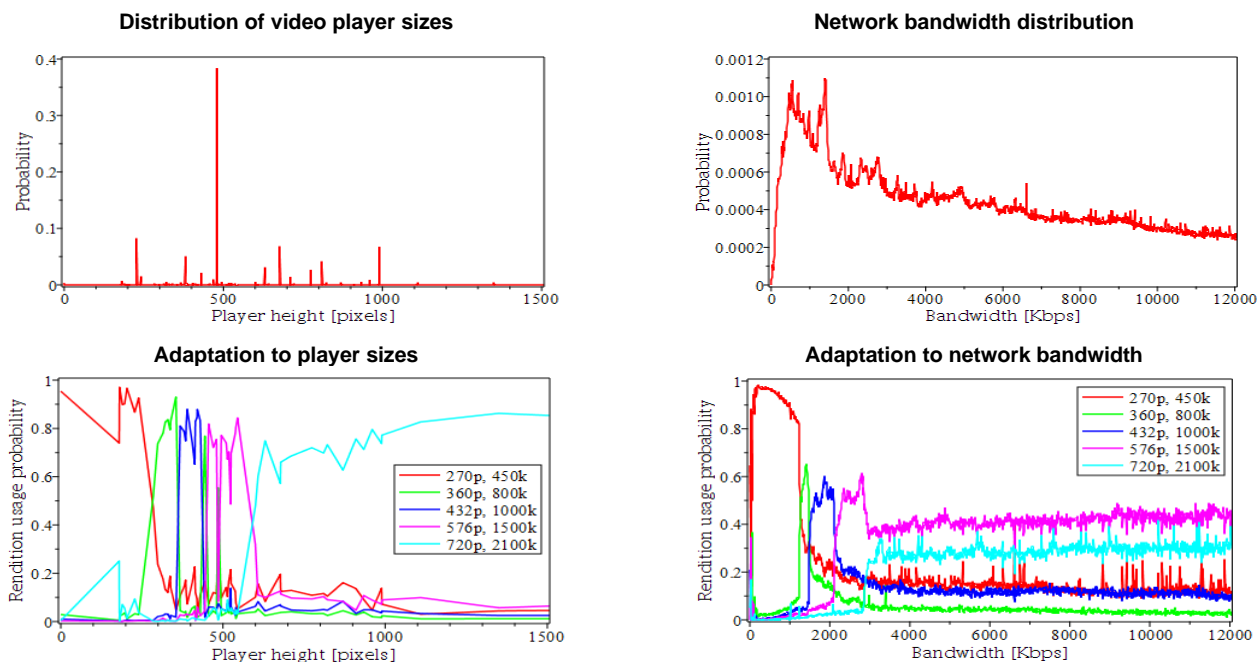


Fig. 1. Playback statistics captured during a large scale live streaming event.

encoded streams used for this event. The playback statistics data used in this example are provided in [8].

TABLE I. ABR LADDER USED FOR STREAMING OF THE EVENT.

Rendition	Codec	Profile	Resolution	Framerate	Bitrate
1	H.264	Baseline	480x270	23.976	450k
2	H.264	Baseline	640x360	23.976	800k
3	H.264	Main	768x432	23.976	1000k
4	H.264	Main	1024x576	23.976	1500k
5	H.264	Main	1280x720	23.976	2100k

As shown in Fig. 1, the distribution of player resolutions exhibits several highly distinct peaks, with 480p being the most pronounced. We also see that player sizes do have a significant impact on stream selection logic. E.g., from the bottom left plot, we see that 270p rendition was loaded most frequently when player window sizes were about 300 lines or less. Similarly, 720p rendition was loaded most frequently when player sizes were about 600 lines and beyond. From the bottom right plot, we further see that, as expected, clients also switch streams based on the available network bandwidth. However, in the high-bitrate regime, we notice that it is not the highest bitrate stream (720p, 210Kbps) that becomes used exclusively, but rather a particular mix of all renditions, apparently shaped by the distribution of player sizes.

In other words, we see that player sizes significantly affect the choices of streams used by the system. In this paper, we will try to explain the above-observed effects. We will approach this problem mathematically, by first offering a simple deterministic player model, and then by using probabilistic techniques to derive conditional probabilities of rendition loads under certain assumptions about statistical behavior of networks bandwidth and player sizes. We will then study differences between the predicted and the observed behavior. Additional applications of the proposed model will also be discussed.

### B. Prior and related work

Most early studies on adaptive streaming systems have focused on network-related issues: congestions, packet losses, CDN cache misses, etc. [1-3,9]. Rate adaptation algorithms have also been in focus [10-12]. The fact that content can be different has also been exploited, producing so-called “per-title” [13], “content-aware” [14], and “context-aware” techniques [15-18]. Earlier uses of probabilistic techniques and idealized client models can be found in [15,16,18]. However, most of these results have been obtained under the assumption that streaming clients are adapting only to network bandwidth. Adaptation to player sizes, as we have just observed, makes system behavior much more complex. This paper focuses on the derivation of an adequate client model. Applications of this proposed model for the analysis and optimizations of such systems will be discussed in detail in forthcoming papers [19,20].

### C. Outline

This paper is organized as follows. In Section II we offer definitions of the most involved variables and stochastic models. In Section III, we introduce our model of the client. In Section IV we will use this model to compute rendition load probabilities and compare them to the experimental results. In

Section V we will discuss applications of this proposed model. In Section 6, we will offer conclusions.

## II. DEFINITIONS

### A. Encoding ladders

By an *encoding profile* or a *ladder*, we will understand is a set of video resolutions and bitrates at which a given video asset is encoded for streaming:

$$(W_i \times H_i, R_i), \quad i = 1, \dots, n. \quad (1)$$

Here  $W_i$  denotes video width [in pixels],  $H_i$  denotes video height [in pixels], and  $R_i$  denotes bitrate [in Kbps] of each rendition. Parameter  $n$  denotes the number of renditions in the ladder. Parameter  $i$  denotes rendition index.

For simplicity, we will also assume that the aspect ratios  $W_i/H_i$  of all renditions in a ladder are the same. Therefore, specification of a single resolution parameter, e.g., height  $H_i$  is sufficient.

We will further say that the ladder is *proper* if bitrates are strictly increasing  $0 < R_1 < \dots < R_n$ , and resolutions are non-decreasing  $0 < H_1 \leq \dots \leq H_n$  for all renditions in the ladder. Table 1 represents an example of a proper ladder.

### B. Player sizes

By  $W_p \times H_p$  we will denote the width and the height [in pixels] of a player. For simplicity, we will also assume that player size has the same aspect ratio as video, and therefore specification of only player height  $H_p$  is sufficient.

When working with a *population* of streaming clients and viewers of the content, we will be dealing with a *set*  $\mathcal{H}_p$  of possible player sizes  $H_p \in \mathcal{H}_p$  that may be selected by different viewers. Furthermore, to model that such different player sizes may be selected with different probabilities, we will assume that  $H_p$  is a *discrete random variable* with a certain probability mass function  $q(H_p)$ , defined over  $\mathcal{H}_p$ .

An example of the distribution of player sizes observed in practice is provided in the top left subfigure in Fig. 1.

### C. Network bandwidth

By  $B$  we will denote network bandwidth value [in Kbps] that may be observed (or measured) by a streaming client.

To enable the probabilistic study of the streaming system, we will further assume that  $B$  is a *continuous random variable* with a certain given probability density function  $p(B)$  and support  $[0, \infty)$ .

An example of the distribution of network bandwidth values as measured by a population of streaming clients in practice is provided in the top right subfigure in Fig. 1.

## III. THE PROPOSED CLIENT MODEL

As we have already seen in Fig. 1, it appears that practical web streaming clients make decisions about which streams to use based at least on two parameters: available network

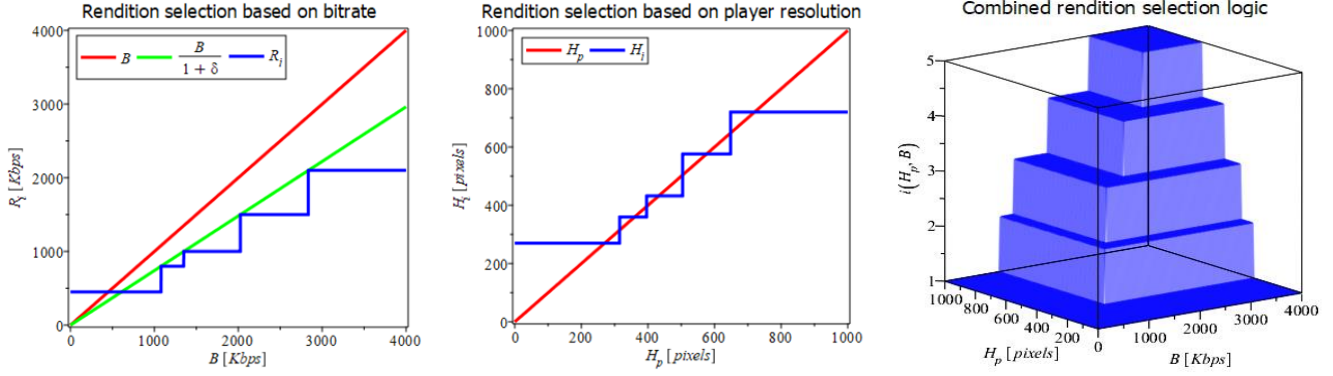


Fig. 2. Construction of streaming client model. Left: rendition selection based on the available network bandwidth  $B$ . Middle: rendition selection based on player window size  $H_p$ . Right: the combined rendition selection logic.

bandwidth  $B$ , and player window size  $H_p$ . To capture this behavior, we will first propose adaptation models for each of these variables separately and then offer a combined model.

To describe client adaptation to network bandwidth, we will use the following model:

$$i_B(B) = \begin{cases} 1 & \text{if } B < T_1^B \\ i & \text{if } T_i^B \leq B < T_{i+1}^B, \quad i = 2, \dots, n-2, \\ n & \text{if } B \geq T_{n+1}^B \end{cases} \quad (3)$$

$$T_i^B = (1 + \delta)R_{i+1}, \quad i = 1..n-1, \quad (4)$$

where  $i_B(B)$  denotes the index of rendition selected,  $B$  is the available network bandwidth,  $R_i$  are ladder bitrates,  $T_i^B$  are bandwidth decision thresholds, and where  $\delta \geq 0$  is a ‘‘bandwidth overhead’’ constant, used to characterize the extent to which a client is trying to utilize all available bandwidth.

We show the plot of this model function in the left subfigure of Fig. 2. The plot is rendered for  $\delta = 0.35$ .

To describe client adaptation to player window, we will use the following model:

$$i_H(H_p) = \begin{cases} 1 & \text{if } H_p < T_1^H \\ i & \text{if } T_i^H \leq H_p < T_{i+1}^H, \quad i = 2, \dots, n-2, \\ n & \text{if } H_p \geq T_{n+1}^H \end{cases} \quad (5)$$

$$T_i^H = \alpha H_i + (1 - \alpha)H_{i+1}, \quad i = 1..n-1 \quad (6)$$

where  $i_H(H_p)$  denotes the index of rendition selected,  $H_p$  is the player height,  $H_i$  are the heights of renditions in the ladder,  $T_i^H$  are the player resolution-based decision thresholds, and where  $\alpha \in (0,1)$  is a constant describing the client’s preference towards downscaling vs. upscaling.

We show the plot of this model function in the middle subfigure of Fig. 2. The plot is rendered for  $\alpha = 0.5$ .

Finally, when we consider adaptation to both network and player-size parameters, we will assume that player logic will be to pick the ‘‘safer’’ choice:

$$i(B, H_p) = \min \{ i_B(B), i_H(H_p) \}. \quad (7)$$

As easily observed, with a proper ladder, this logic results in the selection of renditions with rates always below the available network bandwidth, and resolutions below decision points based on player window size. We plot this model function in the right subfigure in Fig. 2.

In passing, we must note that the proposed client model (7) is indeed extremely simple. It is simply a function of two parameters: bandwidth  $B$  and player size  $H_p$ . This model has no state and no dependencies on buffer size, current buffer fullness, and various additional parameters that all normal implementations of streaming clients would have. However, as we will show in the next section, even such a basic and simple model is sufficient to predict several key effects that we have observed in the real-world playback statistics with web players.

#### IV. MODEL FITTING AND ACCURACY ANALYSIS

##### A. Rendition load probabilities

Given out introduced client model  $i(B, H_p)$ , as well as assumed probabilistic behavior of player sizes  $H_p$  and network bandwidth  $B$ , we can next write formulae for conditional probabilities of loading of  $k$ -th rendition:

$$P(k | H_p) = \int_{B: i(B, H_p)=k} p(B) dB, \quad k = 1, \dots, n \quad (8)$$

$$P(k | B) = \sum_{H_p: i(B, H_p)=k} q(H_p), \quad k = 1, \dots, n \quad (9)$$

In these formulae, the ranges of integration or summation are the regions of values of  $B$  or  $H_p$  such that the index of rendition that becomes selected is  $k$ .

The derived expressions conditional probabilities (8,9) define possible analytical models for the same quantities that we empirically measured and shown earlier in lower subfigures of Fig. 1.

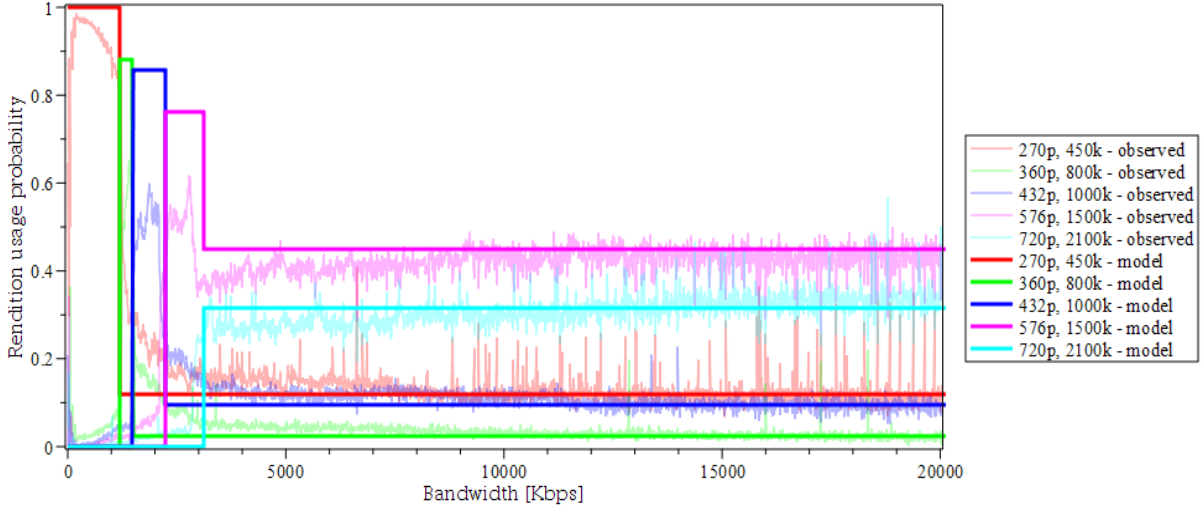


Fig. 3. Observed vs model-predicted conditional probabilities of loading of each rendition.

### B. Streaming data set. Empirical load probabilities.

In [8], we provide a set of playback statistics collected during a large-scale streaming event. For streaming of this event, Brightcove VideoCloud system [6] was used, employing players built using the open-source *video.js* player framework [7]. VideoCloud Analytics system [6] was used to capture the playback statistics.

Specific data provided in the repository [8] include:

- encoding ladder information (cf. Table 1),
- raw player logs, reporting player parameters reported at each 10sec events during playback,
- as well as derived empirical distributions (histograms):
  - o  $\hat{p}(B)$  – network bandwidth histogram,
  - o  $\hat{q}(H_p)$  – histogram of player sizes,
  - o  $\hat{P}(k | B)$  – conditional load probabilities of each rendition w.r.t. network bandwidth, and
  - o  $\hat{P}(k | H_p)$  – conditional load probabilities of each rendition w.r.t. player sizes.

Overall, the dataset [8] provides records of over 200M of client events, which we feel is sufficient for reliable estimation of rendition load probabilities and other performance statistics.

### C. Fitting the player model to empirical statistics

Recall, that our proposed player model (7) uses 2 tuning parameters:  $\alpha$  and  $\delta$ . In order to find them, we will need to minimize the differences between the model probabilities  $P(k | B) = P(k | B, \alpha, \delta)$  and corresponding empirical values  $\hat{P}(k | B)$  provided in the dataset [8].

We use the following objective function:

$$\Phi(\alpha, \delta) = \sum_B \hat{p}(B) \sum_{k=1}^n |P(k | B, \alpha, \delta) - \hat{P}(k | B)| \quad (10)$$

where the summation is done over distinct bandwidth values  $B$  as reported in the dataset [8], and where  $\hat{p}(B)$  represents

empirically measured probability of occurrence of bandwidth value  $B$ . This objective function (10) can be understood as the average variational distance between empirical and model-derived distributions. We note that in the computation of model-based probabilities (9) we used the support set  $\hat{\mathcal{H}}_p$  and empirical player size distribution  $\hat{q}(H_p)$  as provided by the same dataset [8].

In order to solve the optimization problem:

$$\Phi(\alpha^*, \delta^*) = \min_{\alpha, \delta} \Phi(\alpha, \delta). \quad (11)$$

we used brute force enumeration, which with a precision of  $1e-3$  has yielded  $\alpha^* = 0.723$ , and  $\delta^* = 0.45$ .

### D. Model accuracy

In Fig 3. we present the superimposed plots of real-word and model-predicted conditional probabilities  $P(k | B)$  computed by using our model with optimal choice of model parameters  $\alpha$  and  $\delta$ . The fit accuracy is further investigated and reported by using 4 different distance metrics [19] in Table 2. Such metrics were computed for each bandwidth value  $B$ , and subsequently averaged across the range of bandwidth values and by using density  $\hat{p}(B)$ .

TABLE II. MODEL FIT ACCURACY.

Metric	Accuracy
Average L1 norm (variational distance)	0.176283
Average L2 norm	0.101642
Average Information Divergence $D(\hat{P}  P)$	0.205428
Average Kolmogorov-Smirnov test	0.073857

Based on plots in Fig. 3, it can be observed that the proposed client model, despite its extreme simplicity, predicts several key phenomena reasonably well. Thus, it can be observed, that the rendition switch positions along bandwidth  $B$  are well aligned with the corresponding changes in the client-reported statistics. We also notice, that in the high-bandwidth

regime this model captures very well the behavior of the real-world system. In other words, this model explains sufficiently well why web-clients may not use high bitrate renditions even in the excess of bandwidth available.

By studying plots in Fig. 3, we also notice several additional effects that our simple client model does not capture. For example, we notice that real-world rendition selection windows not only do not have sharp vertical boundaries, but they are not even symmetric! The switch-down transition in player statistics seems to be more spread. Indeed, most of such extra detail can easily be captured by making the client model non-deterministic, i.e., treating it as a random process, with a particular density over  $(B, H_p)$  space. However, moving along this path is unlikely to achieve much from a methodological standpoint. The simple model that we have now is both intuitive and performs reasonably well to support some useful applications.

## V. APPLICATIONS

### A. Average performance analysis of streaming systems

The proposed client model can be easily used to derive the precise expressions for many average performance parameters of streaming systems. For example, the *average bitrate* consumed by the streaming system can be expressed as follows:

$$\bar{R} = \int_0^{\infty} p(B) \sum_{H_p \in \mathcal{H}_p} q(H_p) R_{i(B, H_p)} dB, \quad (12)$$

where  $R_i$  denotes bitrate of rendition selected given each combination of bandwidth  $B$  and player size  $H_p$  and where integration and summation are done for both. Similarly, we can produce expression for the *average quality* achieved in the system:

$$\bar{Q} = \int_0^{\infty} p(B) \sum_{H_p \in \mathcal{H}_p} q(H_p) Q(H_{i(B, H_p)}, H_p, R_{i(B, H_p)}) dB, \quad (13)$$

where  $Q(H_i, H_p, R_i)$  is a model of quality for encoded and delivered stream, given its encoded resolution  $H_i$ , bitrate  $R_i$ , and player size  $H_p$ . Again, our client model (9) is utilized here to obtain both selected stream resolution and bitrate. Additional details about suitable for this purpose quality metric and performance analysis of streaming systems can be found in [19].

### B. Design of optimal ladders for web streaming

Given the above-derived expressions for the average quality delivered by the streaming system (13), the problem of finding parameters of an encoding ladder:  $H_1, \dots, H_n$  and  $R_1, \dots, R_n$  maximizing such average quality can be posed. Additional details about the setting of such an optimization problem and finding its solution can be found in [20].

## VI. CONCLUSIONS

In this paper, we have studied the behavior of a streaming system delivering videos embedded in web pages. We have noticed that client adaptation logic in such systems is influenced not only by the available network bandwidth but also by the size of the player window (or viewport of a web page) on the screen.

To study this phenomenon, we have introduced a simple analytical model of streaming clients using adaptation to both of these parameters, and then studied its accuracy relative to statistics of player behavior observed in practice. This study has shown that the proposed model approximates real player behavior reasonably well. Possible uses of this proposed client model for the analysis and optimization of streaming systems have also been discussed.

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